Modeling Hadronic Gamma-ray Emissions from Solar Flares and Prospects for Detecting Non-thermal Signatures from Protostars

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ABSTRACT

We investigate gamma-ray emission in the impulsive phase of solar flares and the detectability of nonthermal signatures from protostellar flares. Energetic solar flares emit high-energy gamma rays of GeV energies, but their production mechanism and emission site are still unknown. Young stellar objects, including protostars, also exhibit luminous X-ray flares, but the triggering mechanism of the flaring activity is still unclear due to the strong obscuration. Non-thermal signatures in mm/sub-mm and gamma-ray bands are useful to probe protostellar flares owing to their strong penetration power. We develop a non-thermal emission model of the impulsive phase of solar flares, where cosmic-ray protons accelerated at the termination shock produce high-energy gamma rays via hadronuclear interaction with the evaporation plasma. This model can reproduce gamma-ray data in the impulsive phase of a solar flare. We apply our model to protostellar flares and show that Cherenkov Telescope Array will be able to detect gamma rays of TeV energies if particle acceleration in protostellar flares is efficient. Non-thermal electrons accelerated together with protons can emit strong mm and sub-mm signals via synchrotron radiation, whose power is consistent with the energetic mm/sub-mm transients observed from young stars. Future gamma-ray and mm/sub-mm observations from protostars, coordinated with a hard X-ray observation, will unravel the triggering mechanism of non-thermal particle production in protostellar flares.

Keywords: Solar flares (1496), Stellar flares(1603), Protostars (1302), Gamma-ray transient sources (1853), Non-thermal radiation sources (1119), Radio transient sources(2008)

1. INTRODUCTION

Solar flares are transient phenomena caused by sudden magnetic energy release at the solar surface (see e.g., Shibata & Magara 2011; Hudson 2011; Cheung & Isobe 2014; Benz 2017, for reviews). They produce broadband photons from radio to high-energy (> 100 MeV) gamma rays by various emission mechanisms. The magnetic reconnection heats up the plasma in the corona and chromosphere, which results in bright optical/ultraviolet/soft X-ray emission. The magnetic reconnection also accelerates non-thermal electrons, which emit hard X-ray and radio signals (Masuda et al. 1994; Chen et al. 2015; Oka et al. 2018).

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The Fermi satellite has been detecting high-energy gamma rays ($E_{\gamma} > 100 \text{ MeV}$) from solar flares (Ajello et al. 2021). The gamma-ray emission episodes can be divided into two phases: the impulsive and gradual phases lasting for $\sim 3-10$ minutes and $\sim 2-20$ hours, respectively. In both phases, the high-energy gamma-ray flux is higher than the extrapolation of the hard X-ray power-law spectrum (e.g., Ackermann et al. 2017), which indicates that the production mechanism of the gamma rays differs from that of the hard Xrays. Hadronic emissions by energetic protons is a viable mechanism of the gamma-ray production (e.g., Kafexhiu et al. 2018), suggesting that the solar flares can accelerate protons up to GeV energies. However, the proton acceleration and subsequent gamma-ray emission mechanisms are still unclear. The long duration of the gradual phase might favor continuous proton acceleration, which can be related to coronal mass ejection (CME) and its subsequent interaction with the ambient plasma

(e.g., Ajello et al. 2014; Petrosian 2016). On the other hand, recent multi-wavelength analysis suggests multiple particle acceleration sites during the solar flares, and the termination shock at the loop top is a plausible proton acceleration site in the impulsive phase (Kocharov et al. 2021). The non-thermal electron production at the termination shock is actively discussed (Masuda et al. 1994; Chen et al. 2015), but the proton acceleration and gamma-ray emission there has yet to be investigated in detail.

Young stellar objects (YSOs) also exhibit flaring activities in X-ray bands in all the stages of their evolution: from the protostar phase (class-0/class-I) to the pre-main sequence phase (class-II/class-III) (Koyama et al. 1996; Feigelson & Montmerle 1999; Feigelson et al. 2002a; Stelzer et al. 2007; Grosso et al. 2020). Compared to solar flares, X-ray flares from YSOs are energetic and frequent. Their total X-ray energy reaches $\mathcal{E}_X \simeq 10^{35} - 10^{37}$ erg, which is likely a small fraction of the total radiation energy and released magnetic energy (see, e.g., Emslie et al. 2012, for solar flares). This indicates that protostellar flares are about $10^4 - 10^6$ times more energetic than the largest recorded solar flares (e.g., Cliver & Dietrich 2013). However, the triggering mechanism of the YSO flares, especially in the protostellar phase, are still controversial.

YSO flares affect the thermochemical structure in the star forming regions by producing strong X-rays. Theoretical studies argue that strong X-rays can change the abundance ratio of molecules such as gas-phase H₂O in the protostellar envelopes (Stäuber et al. 2005, 2006; Notsu et al. 2021) and protoplanetary disks (Waggoner & Cleeves 2019). X-rays by YSO flares can affect the location of snow lines, and recent radio observations suggesting the lack of water vapor can be consistent with the argument (Harsono et al. 2020).

YSO flares are also expected to accelerate cosmic rays (CRs), which also affect the chemical structure by ionizing the gas and destructing molecules (see, e.g., Padovani et al. 2020, for a recent review). Nevertheless, the CR production efficiency in the YSO flares are unknown. Since YSO flares are much more energetic than solar flares, we expect that CR particles can be accelerated to much higher energies. CR protons emit gamma rays via hadronuclear interactions, whereas CR electrons emit mm/sub-mm signals via synchrotron radiation. These signals do not suffer from attenuation even in the dense cold medium, and thus, they are powerful tools to probe the flaring activities and CR productions. Theoretical modelings of non-thermal signatures from YSOs, including emission from jets and magnetospheres, have been discussed (e.g., Araudo et al. 2007;

del Valle et al. 2011; Araudo et al. 2021), but they focus on a specific T-Tauri star or emission from protostellar jets. Detectability of non-thermal signatures from YSO flares in general are not investigated in detail so far.

In this paper, we construct a model of hadronic gamma-ray emission from solar flares, and discuss detectability of non-thermal signatures from protostellar flares. We first model hadronic gamma-ray emission from the impulsive phase of solar flares and calibrate the model parameters using the solar flare data. Then, we apply our model to protostellar flares, and discuss detectability of radio and gamma-ray signals by current and future detectors. Comparison of model prediction with future radio and gamma-ray data will unravel the CR production mechanism in protostellar flares, which may help understand the effects of CRs during the star and planet formation. This paper is organized as follows. In Section 2, we describe our gamma-ray emission model of solar flares. We apply the model to protostellar flares in Section 3. We estimate the synchrotron emission by non-thermal electrons accelerated together with protons in Section 4. Section 5 discusses implications of our results, and Section 6 summarizes our results. We use convention of $A_X = A/10^X$ in cgs unit unless otherwise noted.

2. IMPULSIVE GAMMA-RAY EMISSION MODEL FOR SOLAR FLARES

High-energy gamma rays are accompanied with Mclass $(L_X \sim 3 \times 10^{25} - 3 \times 10^{26} \text{ erg s}^{-1})$ and X-class $(L_X \gtrsim 3 \times 10^{26} \text{ erg s}^{-1})$ flares, and the majority of the gamma-ray detected flares indicate high-velocity CME of $\gtrsim 10^3 \text{ km s}^{-1}$. The peak luminosity of gamma rays from solar flares ranges $L_{\gamma} \sim 5 \times 10^{18} - 5 \times 10^{21} \text{ erg s}^{-1}$ (Ajello et al. 2021). These observations suggest a small gamma-ray to X-ray luminosity ratio, $L_{\gamma}/L_X \sim 10^{-9} 10^{-5}$.

The solar flares are divided into two phases (Kane 1974). One is the impulsive phase in which we observe a rapid and strong variability. Prominent features in this phase are strong hard X-ray and radio signals with a typical duration of a few to ten minutes, which are produced by non-thermal electrons. The other is the gradual phase where the lightcurve slowly evolves for a longer timescale. Bright soft X-ray and H α emissions by thermal hot plasma are observed, which lasts a few to several hours. High-energy gamma rays are accompanied in both phases, though some fraction of gamma-ray flares appear only in either of the phases.

In this section, we construct a model for hadronic gamma-ray emission in the impulsive phase, whose schematic picture is shown in Figure 1. The magnetic re-



Figure 1. Schematic picture of our hadronic gamma-ray emission model from the impulsive phase of solar flares. The magnetic reconnection event produces bipolar outflows. One outflow is ejected to interplanetary space, which is known as CME. The other outflow collides with the magnetic field loops, which leads to the formation of a termination shock. Non-thermal electron beam and thermal conduction by the shocked gas heat up the chromospheric plasma. This leads to the hot plasma upflows (so-called chromospheric evaporation), and the flare loops are filled with the evaporation plasma. In our model, CR protons are accelerated at the shock and confined inside the flare loop owing to the magnetic mirror effect, as seen in the inset of the figure. These CR protons produce hadronic gamma rays via hadronuclear interactions with the evaporation plasma.

connection produces bipolar outflows, and we focus on the sunward outflow colliding with the magnetic field loops. We expect the formation of a termination shock via the collision between the reconnection outflow and flare loops, as some observations suggest (e.g., Aurass et al. 2002; Aurass & Mann 2004).

If non-thermal electrons are accelerated at the termination shock (e.g., Tsuneta & Naito 1998), it is natural to consider that the termination shock also accelerates non-thermal protons. These protons interact with dense plasma evaporated from the chromosphere, which results in hadronic high-energy gamma-ray emission. Throughout this paper, we approximate the flare loop to be a fixed size and filled with uniform plasma for simplicity. In reality, many physical quantities, such as the size of the flare loop and the density of the evaporation plasma, evolve with time. Nevertheless, our treatment provides reasonable agreement with the observational data as shown below.

2.1. Plasma structure during solar flares

Observations of X-class flares, defined by the luminosity in the GOES band (1.55–12.4 keV; $L_X \sim 3 \times 10^{26} - 3 \times 10^{27}$ erg s⁻¹), revealed that the size of the flare loop and the temperature of evaporation plasma are typically $l_{\rm loop} \sim 10^9 - 10^{10}$ cm and $T_{\rm flare} \sim 1 \times 10^7 - 4 \times 10^7$ K, respectively. The durations of the impulsive and gradual phases are typically $t_{\rm imp} \sim 10^2 - 10^3$ sec and $t_{\rm grad} \sim 10^3 - 10^4$ sec, respectively (e.g., Benz 2017). The magnetic field strength and number density of the coronal region can be $B_{\rm rec} \sim 30-300$ G and $n_{\rm rec} \sim 10^8 - 10^9$ cm⁻³ (e.g., Shibata & Magara 2011). We search for the appropriate values of $B_{\rm rec}$ and $n_{\rm rec}$ so that the resulting quantities are in agreement with the observations.

Magnetic reconnection produces bipolar outflows whose velocity is roughly equal to the Alfven velocity around the reconnection region (so-called the inflow region):

$$V_{\rm out} \approx V_A = \frac{B_{\rm rec}}{\sqrt{4\pi m_p n_{\rm rec}}} \simeq 6.9 \times 10^8 B_{\rm rec,2} n_{\rm rec,9}^{-1/2} \,\mathrm{cm \, s^{-1}},$$
(1)

where m_p is the proton mass. The width of the sunward reconnection outflow is estimated to be $l_{out} \sim \eta_{rec} l_{loop} \sim$ $1.0 \times 10^8 l_{loop,9.5} \eta_{rec,-1.5}$ cm, where $\eta_{rec} = V_{in}/V_A$ is the reconnection rate and V_{in} is the reconnection velocity. In solar flares, $\eta_{rec} \sim 0.01 - 0.1$ is observationally estimated (e.g., Isobe et al. 2005; Narukage & Shibata 2006; Takasao et al. 2012). The duration of the reconnection event is given by

$$t_{\rm rec} = \frac{l_{\rm loop}}{V_{\rm in}} \approx 1.4 \times 10^2 l_{\rm loop, 9.5} n_{\rm rec, 9}^{1/2} B_{\rm rec, 2}^{-1} \eta_{\rm rec, -1.5}^{-1} \, \text{s.} \tag{2}$$

This is the typical timescale on which the plasma around the reconnection region brings the magnetic field to it. This timescale corresponds to the duration of the impulsive phase, i.e., $t_{\rm imp} \approx t_{\rm rec}$.

The reconnection heats up the outflow plasma, but the heated plasma cools down via the thermal conduction¹. Then, by considering the balance between the reconnection heating and the conduction cooling, the temperature in the outflow is estimated to be (Yokoyama & Shibata 2001; Shibata & Yokoyama 2002)

$$T_{\rm out} \approx \left(\frac{B_{\rm rec}^3 l_{\rm loop}}{2\kappa_0 \sqrt{4\pi m_p n_{\rm rec}}}\right)^{2/7},\tag{3}$$

where we use the Spitzer thermal conduction coefficient, $\kappa = \kappa_0 T^{5/2}$ with $\kappa_0 \simeq 10^{-6}$ in cgs unit. With this temperature, the outflow is supersonic, and thus, the outflow forms a termination shock when it collides with the reconnected field lines as long as the guide field is weaker than the reconnecting field. The acoustic Mach number of the termination shock is estimated to be (Seaton & Forbes 2009; Takasao & Shibata 2016)

$$M_f \approx \frac{V_{\text{out}}}{C_s} \simeq 5.8 l_{\text{loop},9.5}^{-1/7} B_{\text{rec},2}^{4/7} n_{\text{rec},9}^{-3/7} \propto l_{\text{loop}}^{-2/7} \beta_{\text{rec}}^{-2/7} n_{\text{rec}}^{-1/7},$$
(4)

where $C_s \approx \sqrt{\gamma k_B T_{\text{out}}/m_p}$ is the sound speed, $\gamma = 5/3$ is the specific heat ratio, k_B is the Boltzmann constant, and β_{rec} is the plasma beta for the pre-reconnection plasma. The values of M_f for typical parameters in solar flares are high enough to form a collisionless shock (Treumann 2009) and accelerate particles (Vink & Yamazaki 2014).

In solar flares, the energy released around the shock is transported to the chromosphere by non-thermal electron beams and thermal conduction, which evaporates the chromospheric plasma. The evaporation plasma fills the flare loop, whose temperature is estimated based on MHD simulations with thermal conduction (Yokoyama & Shibata 2001):

$$T_{\rm evap} \approx \frac{T_{\rm out}}{3} \simeq 3.4 \times 10^7 l_{\rm loop, 9.5}^{2/7} B_{\rm rec, 2}^{6/7} n_{\rm rec, 9}^{-1/7} \,\mathrm{K},$$
 (5)

where the factor of 1/3 comes from the numerical result. The density of the evaporation plasma can be estimated by the balance between the magnetic pressure and the gas pressure (Shibata & Yokoyama 2002):

$$n_{\rm evap} \approx \frac{B_{\rm rec}^2}{16\pi k_B T_{\rm evap}} \simeq 4.2 \times 10^{10} B_{\rm rec,2}^{8/7} l_{\rm loop,9.5}^{-2/7} n_{\rm rec,9}^{1/7} \,\rm cm^{-3}$$
(6)

The evaporation plasma emits soft X-rays by thermal bremsstrahlung as observed in the soft X-ray band. The thermal free-free luminosity from the evaporation plasma is estimated to be (Rybicki & Lightman 1979)

$$L_{\rm ff} \simeq 1.7 \times 10^{-27} \times f_{\rm vol} l_{\rm nl} l_{\rm loop}^2 n_{\rm evap}^2 T_{\rm evap}^{1/2} \, {\rm erg \ s^{-1}}$$
(7)
$$\simeq 5.6 \times 10^{26} l_{\rm loop, 9.5}^{18/7} B_{\rm rec, 2}^{19/7} n_{\rm rec, 9}^{3/14} f_{\rm vol, -0.5} f_{\rm nl, 0.5} \, {\rm erg \ s^{-1}},$$

where $f_{\rm vol}$ is the volume filling factor of the evaporation plasma, $l_{\rm nl}$ is the length of the magnetic neutral line, and $f_{\rm nl} = l_{\rm nl}/l_{\rm loop}$ (see Figure 1). This value of $L_{\rm ff}$ corresponds to an X-class flare, with which GeV gamma rays are most frequently accompanied. The cooling timescale of the evaporation plasma is estimated to be

$$t_{\rm ff} = \frac{3}{2} \frac{n_{\rm evap} k_B T_{\rm evap} f_{\rm vol} l_{\rm loop}^2 l_{\rm nl}}{L_{\rm ff}}$$
(8)
$$\simeq 1.7 \times 10^4 l_{\rm loop, 9.5}^{1/7} B_{\rm rec, 2}^{-5/7} n_{\rm rec, 9}^{-3/14} \, {\rm s}.$$

The evaporation plasma falls back to the stellar surface in $t_{\rm ff}$, and this timescale corresponds to the duration of the gradual phase, i.e., $t_{\rm grad} \approx t_{\rm ff}$.

The evaporation plasma will fill a large portion of the reconnected magnetic loop within the travel timescale of the reconnection outflow. The chromospheric evaporation starts to occur in a timescale of non-thermal electron traveling across the loop, $t_{\rm nte} \approx l_{\rm loop}/c \simeq 0.1 l_{\rm loop,9.5}$ s, or the conduction cooling timescale, $t_{\rm cond} \approx \max(t_{\rm nte}, n_{\rm rec} k_B l_{\rm loop}^2/(\kappa_0 T_{\rm out}^{5/2}))$. With our reference parameters, $t_{\rm cond} \simeq t_{\rm nte}$ is satisfied. These timescales are much shorter than the outflow travel timescale,

$$t_{\rm trav} = \frac{l_{\rm rec}}{V_{\rm out}} = 9.2 l_{\rm loop, 9.5} B_{\rm rec, 2}^{-1} n_{\rm rec, 9}^{1/2} f_{h, 0.3} \, s, \qquad (9)$$

where $l_{\rm rec}$ is the position of the reconnection point above the loop top and $f_h = l_{\rm rec}/l_{\rm loop}$. Thus, we can regard that the chromospheric evaporation occurs immediately after the magnetic reconnection. The timescale for the evaporation plasma to fill the loop is estimated as

$$t_{\rm evap} = \frac{l_{\rm loop}}{C_s} = 46 l_{\rm loop,9.5}^{6/7} B_{\rm rec,2}^{-3/7} n_{\rm rec,9}^{1/14} \, \rm s, \qquad (10)$$

¹ Here, we consider the conduction cooling only by thermal electrons for simplicity. In reality, non-thermal electron beam also carries energy away from the outflow plasma.

where we approximate the upflow speed of the evaporation plasma to be the sound speed corresponding to the temperature of $T_{\rm evap}$. The ratio of $t_{\rm evap}$ to $t_{\rm trav}$ can be written as

$$\frac{t_{\rm trav}}{t_{\rm evap}} \simeq 0.20 l_{\rm loop,9.5}^{-1/7} B_{\rm rec,2}^{4/7} n_{\rm rec,9}^{-3/7} f_{h,0.3}.$$
 (11)

Therefore, we expect that a non-negligible portion of the reconnected field line is filled with the evaporation plasma when this reconnected field passes through the termination shock. This picture is consistent with 2-D MHD simulations (Takasao et al. 2015). Protons accelerated at the termination shock will interact with the evaporation plasma as discussed in Section 2.2.

Based on this scenario, the total released energy by reconnection is

$$E_{\rm tot} \approx \frac{l_{\rm loop}^2 l_{\rm nl} B_{\rm rec}^2}{8\pi} \simeq 4.0 \times 10^{31} l_{\rm loop, 9.5}^3 B_{\rm rec, 2}^2 f_{\rm nl, 0.5} \text{ erg.}$$
(12)

Changing $B_{\rm rec}$, $l_{\rm loop}$, and $n_{\rm rec}$, we can reproduce the relation between the released energy and M- and X-class flares given in Maehara et al. (2015). The total thermal energy of the evaporation plasma is

$$E_{\rm evap} \approx l_{\rm loop}^2 l_{\rm nl} \frac{3}{2} n_{\rm evap} k_B T_{\rm evap}$$
(13)

$$\simeq 9.4 \times 10^{30} f_{\rm vol,-0.5} l_{\rm loop,9.5}^3 B_{\rm rec,2}^2 f_{\rm nl,0.5} \text{ erg.}$$

Since the parameter dependence of these two energies are the same except for $f_{\rm vol}$, $E_{\rm tot} > E_{\rm evap}$ is satisfied as long as we choose $f_{\rm vol} < 1$.

2.2. Hadronic emission

To obtain the gamma-ray spectrum of a solar flare, we consider the transport equation for CRs in the flare loops with the one-zone approximation:

$$\frac{\partial N_{E_p}}{\partial t} - \frac{\partial}{\partial E_p} \left(\frac{E_p N_{E_p}}{t_{\text{cool}}}\right) = -\frac{N_{E_p}}{t_{\text{esc}}} + \dot{N}_{E_p,\text{inj}}, \quad (14)$$

where E_p is the proton energy, $N_{E_p} = dN/dE_p$ is the number spectrum for CR protons, $t_{\rm cool}$ is the cooling timescale, $t_{\rm esc}$ is the escape time from the radiation region (i.e., the escape timescale from the flare loop), and $\dot{N}_{E_p,\rm inj}$ is the injection term. We explain the individual term in the following paragraphs.

First, we describe the injection term. We consider that CR particles are accelerated at the termination shock and advected to the flare loop by turbulent motion. The acceleration time is given by (e.g., Drury 1983),

$$t_{\rm acc} \approx \frac{20\xi E_p}{3eB_{\rm rec}c} \left(\frac{c}{V_A}\right)^2,\tag{15}$$

where ξ is the Bohm factor (physically, the mean free path of protons divided by the gyro radius). The advection timescale can be evaluated using the shock width and the outflow velocity to be

$$t_{\rm sh} \approx \frac{l_{\rm out}}{V_{\rm adv}} \simeq 0.14 l_{\rm loop, 9.5} B_{\rm rec, 2}^{-1} n_{\rm rec, 9}^{1/2} \eta_{\rm rec, -1.5} f_{\rm adv}^{-1} \, \text{sec},$$
(16)

where $V_{adv} = f_{adv}V_A$ is the advection velocity at the shock downstream and f_{adv} is a parameter. The diffusive shock acceleration process accelerates CR protons with a power-law energy distribution below the maximum energy given by balancing t_{sh} and t_{acc} . The maximum energy is estimated to be

$$E_{p,\max} \approx \frac{3eB_{\rm rec}V_A l_{\rm out}}{20\xi'c}$$
(17)
$$\simeq 5.1B_{\rm rec,2}^2 n_{\rm rec,9}^{-1/2} l_{\rm loop,9.5} \eta_{\rm rec,-1.5} {\xi'}_{0.3}^{-1} \,\,{\rm GeV},$$

where $\xi' = \xi f_{adv}$. Here, we give ξ' as a parameter. This energy is higher than the pion production threshold, $E_{p,thr} \simeq 1.22$ GeV, and thus, these CRs can emit high-energy gamma rays via hadronuclear interactions. In reality, multiple termination shocks may exist above the loop top region (Takasao & Shibata 2016), but we consider the CR particle acceleration at a single shock for simplicity.

Since $t_{\rm sh} \ll t_{\rm rec}$ and $t_{\rm sh} \ll t_{\rm ff}$, we can regard that the CR particles are instantaneously injected to the flare loop with a power-law form of $\dot{N}_{E_p,\rm inj} \propto E_p^{-s}$. The spectral index is given by s = (r+2)/(r-1), where $r = (\gamma+1)/(\gamma-1+2/M_f^2)$ is the compression ratio (e.g., Blandford & Eichler 1987). We obtain $r \simeq 3.67$ and $s \simeq 2.12$ with our reference parameters. We consider the sheet-like geometry of the reconnection outflows and give normalization of the injection term as

$$\int \dot{N}_{E_p,\text{inj}} dE_p = L_p = \epsilon_p n_{\text{rec}} m_p V_A^3 l_{\text{nl}} l_{\text{out}}$$
(18)
$$\simeq 5.5 \times 10^{26} \epsilon_{p,-3} l_{\text{loop},9.5}^2 B_{\text{rec},2}^3 n_{\text{rec},9}^{-1/2} \eta_{\text{rec},-1.5} f_{\text{nl},0.5} \text{ erg s}^{-1}$$

where ϵ_p is the production efficiency of relativistic CRs and L_p is the CR proton luminosity. The termination shock should be an oblique shock in which the magnetic field is almost perpendicular to the shock normal, as shown in MHD simulations (Takasao et al. 2015; Takasao & Shibata 2016; Shen et al. 2018), but the values of ϵ_p in oblique shocks are uncertain. Particle-incell simulations suggest that oblique shocks are likely inefficient to produce CRs (Caprioli & Spitkovsky 2014; Caprioli et al. 2015). On the other hand, some theoretical models argue that oblique shocks can accelerate CR particles more efficiently than parallel shocks (Xu & Lazarian 2022), and observations of supernova remnants support the efficient particle acceleration at perpendicular shocks (West et al. 2017). In this paper, we tune ϵ_p so that the resulting gamma-ray spectrum matches the Fermi-LAT data.

Next, we explain the escape term. In the flare loops, the magnetic field strength at the footpoints is stronger than that in the loop-top region (see the inset of Figure 1). Thus, the flare loops work as a magnetic bottle that confines CRs efficiently (Somov & Kosugi 1997; Aschwanden et al. 1998). The CRs with a small pitch angle can escape from the flare loops, and thus, the timescale of the CR escape should be comparable to that of the pitch-angle scattering (e.g., Stawarz & Petrosian 2008; Kimura et al. 2015):

$$t_{\rm esc} \approx \eta_{\rm turb} \frac{l_{\rm loop}}{c} \simeq 1.1 \eta_{\rm turb, 1} l_{\rm loop, 9.5} \, \mathrm{s}, \qquad (19)$$

where $\eta_{\text{turb}} = B^2/(8\pi \int \mathcal{P}_k dk)$ is the turbulence strength parameter, \mathcal{P}_k is the turbulence power spectrum, and we assume Goldreich-Sridhar turbulence of $\mathcal{P}_k \propto k^{-2}$ (Goldreich & Sridhar 1995). This turbulence power spectrum leads to the hard-sphere type scattering in which the scattering timescale is independent of the particle energy.

Finally, we explain the cooling term. We consider only pp inelastic collisions $(p + p \rightarrow p + p + \pi)$, because other processes, such as photomeson production $(p + \gamma \rightarrow p + \pi)$, Bethe-Heitler $(p + \gamma \rightarrow p + e^+ + e^-)$, and proton synchrotron processes are negligible. Then, the cooling timescale is given by $t_{\rm cool} \approx t_{pp} \approx 1/(n_{\rm evap}\sigma_{pp}\kappa_{pp}c)$, where $\sigma_{pp} \sim 30$ mb and $\kappa_{pp} \simeq 0.5$ are the crosssection and inelasticity for pp inelastic collisions, respectively.

There are three relevant timescales for gamma-ray emission from solar flares. One is the reconnection timescale, $t_{\rm rec}$, which indicates the duration of CR production. Another is the CR escape timescale, $t_{\rm esc}$, after which CRs escape from the emission region. The other is the cooling timescale of the evaporation plasma, $t_{\rm ff}$. after which the target of hadronuclear interactions disappears. For luminous solar flares, $t_{\rm esc} < t_{\rm rec} < t_{\rm ff}$ is always satisfied. Then, the CRs escape from the loop while they are continuously accelerated at the shock and provided into the loop. Thus, the CR spectrum in the loop should be determined by the balance between the injection and escape, $N_{E_p} \approx \dot{N}_{E_p, inj} t_{esc}$, and the steady state is achieved. The CR protons interact with the evaporation plasma and produce charged and neutral pions with the ratio of π^{\pm} : $\pi^0 \sim 2$: 1. Charged pions decay to neutrinos and electrons/positrons, while neutral pions decay to gamma rays. The pion-decay gamma-ray spectra are roughly estimated to be (e.g.,

Murase et al. 2013; Ahlers & Halzen 2017)

$$E_{\gamma}L_{E_{\gamma}} \approx \frac{1}{3} f_{pp} E_p^2 \dot{N}_{E_p,\text{inj}}, \qquad (20)$$

where $E_{\gamma} \approx 0.1 E_p$ is the typical gamma-ray energy produced by pion decay and $f_{pp} = \min(t_{\rm esc}/t_{pp}, 1) \simeq$ $2.4 \times 10^{-5} l_{\rm loop,9.5}^{5/7} B_{\rm rec,2}^{8/7} n_{\rm rec,9.5}^{1/7} \eta_{\rm turb,1}$ is the pion production efficiency. Since the CR spectrum is soft (s > 2) for solar flares, the gamma-ray spectrum has a peak around the pion production threshold, $E_{\gamma,\rm pk} \sim 100$ MeV. The peak luminosity of the pion-decay gamma rays is estimated to be

$$L_{\gamma,\rm pk} \approx \frac{1}{3} f_{pp} L_p \simeq 3.6 \times 10^{21} \tag{21}$$

$$\times \epsilon_{p,-3} l_{\text{loop},9.5}^{19/7} B_{\text{rec},2}^{29/7} n_{\text{rec},9}^{-5/14} \eta_{\text{rec},-1.5} \eta_{\text{turb},1} f_{\text{nl},0.5} \text{ erg s}^{-1}.$$

The estimated gamma-ray luminosity is consistent with the Fermi-LAT observations of the impulsive phase (Ajello et al. 2021).

The pion decay process also produces secondary neutrinos and electron-positron pairs. We cannot expect detection of neutrinos in GeV energies because of the small neutrino-nucleon interaction crosssection and strong atmospheric background. The luminosity of the secondary electron-positron pairs is comparable to the luminosity of gamma rays, which is likely much lower than the primary non-thermal electrons accelerated together with protons (see Section 4). Therefore, we do not discuss the emission by the secondary electron-positron pairs.

To quantitatively compare our model to the observations, we numerically calculate the hadronic gamma-ray spectrum from solar flares. We use the delta-function approximation (Aharonian & Atoyan 2000) with σ_{pp} calibrated by the LHC data (Kafexhiu et al. 2014). The proton spectrum is obtained by solving Equation (14) with a steady state approximation (see, e.g., Kimura et al. 2019, 2020; Kimura & Toma 2020).

Figure 2 exhibits the gamma-ray spectra for our model and for the impulsive phase of a Fermi-LAT solar flare on 2014 February 25 (Ajello et al. 2021). We tabulate our model parameters and resulting quantities in Table 1. Our parameter choice leads to an X-class flare (X2.7), in rough agreement with the observed class (X4.9). Our model can roughly reproduce the observed gamma-ray spectrum with a reasonable parameter set. Chen et al. (2014) estimated the loop size and the density of the X-ray emission region, and our parameter choice is in rough agreement with theirs. Also, Seaton et al. (2017) estimated the reconnection rate in the gradual phase to be $4 \times 10^{-3} - 7 \times 10^{-3}$, which is an order of magnitude lower than that used in our calculations. However, the reconnection rate in the impulsive phase can be higher



Figure 2. High-energy gamma-ray spectra in the impulsive phase of the solar flare on 2014 February 25. The red line is our model prediction, and the grey simbols with error bars are the Fermi-LAT data (Ajello et al. 2021).

than that in the gradual phase (e.g., Takasao et al. 2012; Qiu & Cheng 2022). Therefore, we consider that our parameter choice does not contradict with that by Seaton et al. (2017).

3. APPLICATION TO PROTOSTELLAR FLARES

3.1. The accretion-driven flare scenario

We apply our model to protostellar flares. Our discussion on protostellar flares is based on the scenario proposed by Takasao et al. (2019), which is summarized in Figure 3. They focus on the efficient magnetic transport driven by the disk surface accretion (coronal accretion: Matsumoto et al. 1996; Beckwith et al. 2009; Takasao et al. 2018). The accretion flows carry disk poloidal fields to the protostar, and the large-scale fields are accumulated (panel 1). When the magnetic pressure around the protostar becomes comparable to the disk gas pressure, the protostellar field starts to expand toward the equator. The expanding field interacts with the disk surfaces and exchanges the angular momentum. This reduces the disk surface density around the interacting region, and the protostellar fields expand further from the northern and southern hemispheres. Finally, the protostellar fields reconnect each other around the equatorial plane, which drives a flare (panel 2). The magnetic reconnection releases sufficient magnetic energy to account for powerful X-ray flares with $E_X \sim 10^{37}$ erg.

A magnetic reconnection drives bipolar outflows; one moving toward the protostar and the other heading to the protoplanetary disk (panel 3a). The outflow heading toward the protostar forms the closed magnetic arcade or flare loop. We can regard this closed flare loop as the scale-up version of a solar flare loop. Thus, we can apply our solar flare model to this system (panel 3b), although the triggering mechanism is different from stellar flares. We note that the triggering mechanism of X-ray flares in the more evolved YSOs could be similar to that in the main sequence stars including the Sun (e.g. Getman & Feigelson 2021; Getman et al. 2021). The other outflow colliding with the disk evolves nearly adiabatically because the magnetic field accompanied by the hot plasma is connected to neither the protostellar surface nor the disk gas. In this case, the acoustic Mach number is close to 1 (see Equations (3) and (4)), and thus, we cannot expect particle acceleration at the termination shock.

3.2. Physical quantities around the reconnection region

First, we estimate the physical quantities of the magnetic reconnection region before the reconnection. As a reference parameter set, we take the protostellar mass $M_* = 0.5 M_{\odot}$ and radius $R_* = 2 R_{\odot}$. The magnetic reconnection occurs at a radius of $R_{\rm dis} \sim 2 R_*$. The resulting flare loop will have a size similar to the protostar, i.e., $l_{\rm loop} \sim 10^{11}$ cm.

As pointed out by Takasao et al. (2019), the stellar field strength before a flare is determined by the balance between the magnetic pressure around the poles and the disk gas pressure. This condition is similar to the magnetically arrested disk (MAD) state in black hole accretion (Bisnovatyi-Kogan & Ruzmaikin 1974; Narayan et al. 2003; McKinney et al. 2012). We first estimate the disk gas pressure around $R_{\rm dis}$, and then, calculate the reconnection field strength, $B_{\rm rec}$. The disk density at $R \sim R_{\rm dis}$ can be estimated using the alpha-viscosity prescription:

$$n_d \approx \frac{\dot{M}}{4\pi R_{\rm dis}^2 \alpha \mathcal{H}^3 V_K}$$
(22)
$$\simeq 2.1 \times 10^{16} \dot{M}_{-6.5} M_{-0.3}^{-1/2} R_{\rm dis,0.3}^{-3/2} \mathcal{H}_{-1}^{-3} \alpha_{-1} \text{ g cm}^{-3},$$

where $V_K = \sqrt{GM/R_{\rm dis}} \simeq 2.2 \times 10^7 M_0 R_{\rm dis,0.3} \text{ cm s}^{-1}$ is the Keplerian velocity, $\mathcal{H} = H/R_{\rm dis} \approx C_s/V_K \sim 0.1$ is the disk aspect ratio, M is the mass of the protostar, H is the pressure scale height, C_s is the sound speed in the protoplanetary disk, $R_{\rm dis,0.3} = R/(2R_{\odot})$, $\dot{M}_{-6.5} = \dot{M}/(10^{-6.5} M_{\odot} \text{ yr}^{-1})$, and $M_{-0.3} = M/(0.5 M_{\odot})$. When the magnetic reconnection occurs, the magnetic pressure around the protostar is comparable to the disk

Table 1. List of parameters and resulting physical quantities for solar and protostellar flares. Parameters for the solar flare are calibrated using the data for the event on 2014 February 25. The values for Model C are identical to those for Model B, except for ϵ_p and L_p .

	Given paran	neters												
	Model		l_{1a}	оор	$B_{\rm rec}$	$n_{\rm rec}$		$f_{\rm nl}$	ϵ_p	$\eta_{\rm rec}$	$f_{\rm vol}$	$\eta_{ m turb}$	ξ	ϵ_e/ϵ_p
			$[10^{10}]$	$^{\circ} \text{ cm}]$	[kG]	$[10^9 \text{ cm}^{-3}]$								
	Sun		0.	32	0.10	1.0		6.0	0.004	0.032	0.32	10	2	0.032
	Model A		1	0	1.0	10		1.0	0.004	0.032	0.32	10	2	0.032
	Model B		1	3	2.0	10		1.0	0.004	0.032	0.32	10	2	0.032
	Model (C	1	3	2.0	10		1.0	0.1	0.032	0.32	10	2	0.032
Resulting quantities														
Model	V_A	M_f	s	$\log_{10}(L_{\rm ff})$		$T_{\rm evap}$	t_X	t_{γ}	\log_1	$E_{10}(E_{p,\mathrm{max}})$	$_{x})$ lo	$g_{10}(L_p)$	le	$\log_{10}(\nu_{\rm ssa})$
	$[10^8 \text{ cm s}^{-1}]$			$[\text{erg s}^{-1}]$		$[10^7 K]$	[hr]	[mi	n]	[GeV]		$[\text{erg s}^{-1}]$		[Hz]
Solar Flare	6.9	5.8	2.12	27.02		3.4	4.7 2.4		Ł	0.71		27.62		8.93
Model A	21.8	4.9	2.17	33.03		47.5	2.4	24.	2	3.71		32.34		10.76
Model B	43.7	7.1	2.08	34.14		92.7	1.7	15.	7	4.43		33.47		11.28
Model C	43.7	7.1	2.08	34.14		92.7	1.7	15.7		4.43	34.87			11.67

gas pressure². The magnetic field strength at the magnetic reconnection point is estimated to be

$$B_{\rm rec} \approx \sqrt{8\pi n_d m_p C_s^2} \simeq 1.4 \times 10^3 n_{d,16}^{1/2} M_{-0.3}^{1/2} R_{\rm dis,0.3}^{-1/2} \mathcal{H}_{-1} \,\rm G.$$
(23)

The magnetic reconnection occurs when the disk matter is cleared (see Figure 3). At this stage, the stellar coronal gas expands toward the reconnection point near the equatorial plane. Therefore, the density just around the reconnection region is the coronal value and should be much smaller than the disk density. We assume $n_{\rm rec} = 10^{10} \text{ cm}^{-3}$ as a fiducial value, which is higher than the solar coronal value ($\sim 10^8 - 10^9 \text{ cm}^{-3}$), because of the following reasons. First, protostars typically exhibit stronger magnetic activities than the Sun. Second, more X-ray luminous stars have larger magnetic fluxes (Pevtsov et al. 2003; Takasao et al. 2020). Third, the coronal density in protostars could be enhanced by accretion heating (Cranmer 2008). In the rest of this paper, we provide $l_{\rm loop}, \; n_{\rm rec}, \; {\rm and} \; B_{\rm rec}$ as primary parameters for the magnetic reconnection events so that we can apply the scenario in the previous section.

3.3. Thermal emissions from evaporation plasma

X-ray observations revealed that many protostars exhibit luminous X-ray flares (Imanishi et al. 2001; Pris-

inzano et al. 2008). We search for suitable parameter sets within the range of $B_{\rm rec} = 3 \times 10^2 - 3 \times 10^3$ G, $l_{\text{loop}} = 3 \times 10^{10} - 3 \times 10^{11} \text{ cm}$, and $n_{\text{rec}} = 10^{10} - 10^{11} \text{ cm}^{-3}$ so that our model results are consistent with X-ray observations summarized below. The X-ray luminosity, duration, and temperature of protostellar flares lie in the following ranges: 3×10^{30} erg s⁻¹ $\lesssim L_X \lesssim 10^{34}$ erg s⁻¹, $3 \times 10^4 \text{ s} \lesssim t_X \lesssim 10^5 \text{ s}, 10^7 \text{ K} \lesssim T_{\text{evap}} \lesssim 10^9 \text{ K}$ (Imanishi et al. 2003; Getman et al. 2008; Getman & Feigelson 2021; Getman et al. 2021), where L_X is evaluated in the Chandra band (0.5 keV - 7 keV). MAXI provides an additional constraint on X-ray luminosity. MAXI does not detect any flares from protostars in Taurus Molecular Cloud and Rho Ophuchi Cloud Complex (Tsuboi et al. 2016). Since the cadence of the MAXI observation (once in a 90 min) is shorter than the typical duration of protostellar flares, non-detection means that X-ray emissions from protostellar flares should be lower than the MAXI sensitivity (~ 10^{-9} erg s⁻¹ cm⁻² for the 2 - 20 keV band; Matsuoka et al. 2009).

Table 1 lists the parameter sets whose resulting X-ray fluxes are consistent with the Chandra and MAXI data. Figure 4 shows photon spectra by free-free emission from thermal electrons (see thick-dotted lines) for our protostellar flare models A (red), B (blue), and C (green). The thick dotted lines for models B and C are completely overlapped. The durations of X-ray flares are a few hours, and the temperature of evaporation plasma is $5 \times 10^8 - 9 \times 10^9$ K. The thermal free-free flux below the UV range is lower than those from other components, such as a protostar (thin-dotted line), a protoplanetary

² In black hole accretion flows, we use the critical magnetic flux, $\Phi_{\rm MAD} = 2\pi R_G B_{\rm rec} / \sqrt{\dot{M}c} \sim 50$, to estimate the magnetic fields around black holes (e.g., Yuan & Narayan 2014; Kimura et al. 2022). The order of $\Phi_{\rm MAD}$ is obtained by balancing the magnetic energy and gravitational energy, which is different from Equation (23).



Figure 3. Schematic picture of our scenario of gamma-ray flares from protostars. Panel (1): Mass accretion from a protoplanetary disk accumulates magnetic fields around a protostar. The surface layers of the disk accrete faster than the midplane. This flow structure stretches the magnetic fields. Panel (2): When magnetic field strength becomes comparable to the thermal energy of the disk gas, magnetic fields and the coronal plasma starts to expand toward the disk midplane, which clears out the disk. This eventually triggers magnetic reconnection. Panel (3a): The magnetic reconnection produces bipolar outflows. One moves to the protostar, and it cools down by thermal conduction before colliding with the flare loop. The other outflow moves to the protoplanetary disk, and it evolves adiabatically. Panel (3b): Thermal conduction to the protostellar surface leads to evaporation of the protostellar atmosphere, and the evaporation plasma emits X-rays via thermal bremsstrahlung. Also, the collision between the outflow and the flare loop forms a shock in the outflow, where non-thermal particles are accelerated via the diffusive shock acceleration process. The accelerated protons emit gamma rays and neutrinos via hadronuclear interactions with evaporation plasma, and non-thermal electrons emit mm/sub-mm photons by synchrotron radiation.

disk (gray-shaded region), and protostellar jets (grayshaded region).

3.4. Hadronic gamma-ray emissions

We discuss non-thermal particle acceleration and emissions in protostellar flares. In order to accelerate particles at the shock, the optical depth for the shock upstream should be optically thin (e.g., Murase & Ioka 2013; Kimura et al. 2018a). Otherwise, the photons diffusing from the shock downstream decelerate the upstream fluid significantly. This causes a gradual velocity change at the shock (Budnik et al. 2010; Levinson & Nakar 2020), and CR particles are no longer able to cross the shock. In the pre-shock outflow, the opacity is dominated by the electron scattering (Bell & Lin 1994). The optical depth for the reconnection outflow is estimated to be $\tau_T \approx n_{\rm rec} \sigma_T l_{\rm loop} \simeq 7 \times 10^{-4} n_{\rm rec, 10} R_{\rm rec, 11}$, and



Figure 4. Broadband photon spectra from protostellar flares. The thick-solid, thick-dashed, and thick dotted lines show the hadronic pion-decay, leptonic synchrotron, and thermal free-free components, respectively. The red, blue, and green lines are for Model A, B, and C, respectively. The thermal free-free emission for Model B is identical to that for Model C. The gray-shaded region and grey-thin-dotted line show the disk & Jet components given in AMI Consortium et al. (2012) and the thermal spectrum from the protostar with $R_* = 2R_{\odot}$ and T = 4000 K, respectively. The lightgreen-shaded region shows the flux range of protostellar flare observations by Chandra (Getman et al. 2008, 2021). The magenta-thin-solid lines show the sensitivity curves for MAXI (Matsuoka et al. 2009), e-ASTROGAM (De Angelis et al. 2017), and CTA (Cherenkov Telescope Array Consortium et al. 2019). The thermal free-free components are consistent with the Chandra observations. CTA will be able to detect the hadronic emission for model C. The leptonic synchrotron emission can be detected by mm/sub-mm surveys.



Figure 5. Spectra of injected non-thermal protons. The red-solid, blue-dashed, and green-dotted lines are for models A, B, and C, respectively.

thus, the radiation mediated condition is easily avoided with our reference parameters³.

In the range of our investigation of protostellar flares, $t_{\rm sh} < t_{\rm esc} < t_{\rm rec} < t_{\rm ff}$ is satisfied. This situation is the same as that for solar flares, and thus, we can apply the model discussed in Section 2.2. We find that photomeson production, Bethe-Heitler, and proton synchrotron processes are negligible even with the parameters for protostellar flares.

According to Equations (17) and (18), L_p and $E_{p,\max}$ strongly depend on l_{loop} and B_{rec} . Thus, the protostellar flares can produce cosmic rays and gamma rays much more efficiently, owing to their large loop size and strong magnetic field. We find that the protostellar flares can accelerate protons up to multi-TeV range, as shown in

³ Accretion shocks at the surface of protostars are discussed as a CR production site (e.g., Padovani et al. 2016), but the accretion shocks can be optically thick because the density at the accretion shock can be as high as n_d given in Equation (22). We need to check the radiation-mediated condition when discussing the non-thermal processes in dense environments, which is often ignored in the previous literature.

Figure 5 (see Table 1 for the values of $E_{p,\text{max}}$). These protons can produce very-high-energy (VHE: $E_{\gamma} > 100$ GeV) gamma rays, where the sensitivity to a transient source is better than the lower energy gamma-ray bands.

The gamma-ray luminosity at the VHE range is analytically estimated to be

$$L_{\gamma,\text{vhe}} \approx \frac{1}{3} f_{pp} f_{\text{vhe}} L_p \simeq 1.7 \times 10^{29} l_{\text{loop},11}^{19/7} B_{\text{rec},3}^{29/7} n_{\text{rec},10}^{-5/14} \\ \times \epsilon_{p,-3} \eta_{\text{rec},-1.5} \eta_{\text{turb},1} f_{\text{nl}} \left(\frac{f_{\text{vhe}}}{0.067}\right) \text{ erg s}^{-1}, (24)$$

where $f_{\rm vhe} = ({\rm TeV}/m_p c^2)^{2-s}(s-2)/(1-(E_{p,\max}/m_p c^2)^{2-s})$ is the correction factor from the bolometric luminosity to the VHE range ⁴. The VHE flux is estimated to be

$$F_{\gamma,\text{vhe}} = \frac{L_{\gamma,\text{vhe}}}{4\pi d^2} \simeq 4.6 \times 10^{-15} l_{\text{loop},11}^{19/7} B_{\text{rec},3}^{29/7} n_{\text{rec},10}^{-5/14} \epsilon_{p,-3}$$
$$\times \eta_{\text{rec},-1.5} \eta_{\text{turb},1} f_{\text{nl}} \left(\frac{f_{\text{vhe}}}{0.065}\right) \left(\frac{d}{140 \text{ pc}}\right)^{-2} \text{ erg s}^{-1} \text{ cm}^{-2}$$

where d is the distance to the protostar and we use the distance to the nearby star-forming regions, such as Taurus molecular cloud and Rho Ophiuchi molecular complex. This value is an order of magnitude lower than the sensitivity of CTA ($\sim 10^{-13}$ erg s cm⁻² for a 50-h integration: CTA website). Thus, with these parameters, we cannot expect the VHE gamma-ray detection. We numerically calculate the gamma-ray spectra from the protostellar flare with the method given in Kelner et al. (2006) with pp cross-section given in Kafexhiu et al. (2014), and confirm this conclusion as shown in Figure 4. The result for our reference model (Model A) is indicated by the thick-red-solid line, which is much lower than the sensitivity curves of CTA (thin-magenta curves), respectively.

However, the gamma-ray luminosity strongly depends on the values of $B_{\rm rec}$ and $l_{\rm loop}$, which are largely unknown. Figure 4 also exhibits the GeV-TeV gamma-ray spectra from protostellar flares for other parameter sets tabulated in Table 1. For a moderate case (Model B; high $B_{\rm rec}$ and $l_{\rm loop}$), the VHE flux reaches the sensitivity of CTA. Since the duration of the gamma-ray emission is estimated to be $t_{\gamma} \approx t_{\rm rec} \sim 10^3$ sec as tabulated in Table 1, we can expect detection of VHE gamma rays if we stack ~ 180 protostellar flares. Since the field-ofview (FoV) of CTA is ~ 3 deg × 3 deg, they can monitor ~ 100 - 300 YSOs simultaneously. Since 200-ks observation by Chandra (FoV= 0.29 deg × 0.29 deg) found 71 YSO flares (Imanishi et al. 2001, 2003), we can expect several hundreds or several thousands of YSO flares within the FoV of CTA during the 50-hour integration. Therefore, CTA could detect gamma rays if we perform coordinated observation with a wide-field X-ray satellite and a dedicated data analysis.

The protostellar flares may be able to accelerate CR protons more efficiently than solar flares. The amount of supra-thermal particles in the pre-shock region (i.e., reconnection outflow) is a key to determine the production efficiency of relativistic CRs, ϵ_p . We infer that the protostellar flares will have a higher value of ϵ_p than solar flares, considering the geometry of the reconnecting magnetic fields. Theoretical investigations have suggested that magnetic reconnection with some amount of the guide field accelerates non-thermal particles less efficiently than reconnection without it (e.g. Arnold et al. 2021). Regarding the solar flares, it is expected that coronal reconnecting fields have a strong guide field before the flare onset because the coronal field is generally sheared by photospheric plasma motions (e.g., Schriiver 2007; Toriumi & Takasao 2017). The same will be true for the stellar flares, as their properties are similar to the solar ones (Getman et al. 2021). On the other hand, we consider protostellar flares powered by accretion (Takasao et al. 2019). In this framework, the protostar gains magnetic energy by getting the large-scale poloidal fields from the disk via accretion. In this case, the magnetic reconnection in the protostellar flares occurs with little guide fields (see Panel (2) of Figure $3)^5$. The reconnection with such a configuration will more efficiently produce supra-thermal particles in the reconnection outflow (Arnold et al. 2021; Zhang et al. 2021). Such high-energy particles will be easily re-accelerated via the diffusive shock acceleration (Caprioli et al. 2018). Therefore, protostellar flares can have a higher value of ϵ_p than solar flares. Note that protostellar flares in the magnetospheric accretion paradigm are powered by a different mechanism (e.g. Hayashi et al. 1996; Uzdensky 2004), where the main energy source is twisting of the stellar field by the rotating disk.

Considering the above argument, we also plot the hadronic gamma-ray spectrum for an optimistic case

⁴ $f_{\rm vhe}$ is computed as follows. We use Eq. (18) to obtain the normalization of the CR proton spectrum. The CR proton spectrum has a peak at $E_p \approx m_p c^2$ for s > 2. VHE gamma rays are produced by CR protons of $E_p \gtrsim 1$ TeV, but the number density of protons at this energy is lower than that at $E_p \sim m_p c^2$. We take into account such a reduction of the number of CR protons when computing $f_{\rm vhe}$.

⁵ Although a shear motion exists in the disk, the magnetic reconnection proceeds with a weak guide field component as long as the symmetry across the equatorial plane is not strongly violated (Ripperda et al. 2022).

with $\epsilon_p = 0.1$ (Model C) in Figure 4. In this case, CTA can detect gamma rays from a single protostellar flare without the help of an X-ray satellite. We expect the enhancement of CR production, compared to solar flares, only for the accretion-driven flare scenario. Thus, future VHE gamma-ray observations of protostars may be useful to probe the triggering mechanism of protostellar flares and non-thermal phenomena occurring there.

Hadronic gamma-ray emission is inevitably accompanied by high-energy neutrinos, whose energy and differential luminosity and energy can approximately be written by $E_{\nu} \sim (1/2)E_{\gamma}$ and $E_{\nu}L_{E_{\nu}} \approx (1/2)E_{\gamma}L_{E_{\gamma}}$, respectively. We evaluate the neutrino detectability by current and near-future km³ detectors (Adrián-Martínez et al. 2016; Avrorin et al. 2014; Agostini et al. 2020), but the neutrino fluence from the protostellar flares are too low to detect. We need to stack ~ 10⁵ protostellar flares to detect a single neutrino with km³ detectors, and hence, we cannot expect any neutrino detection even with the future 10-km³ detectors (Aartsen et al. 2022).

4. LEPTONIC EMISSION

In this section, we discuss the detectability of emissions by relativistic electrons. At the termination shock, primary CR electrons can be accelerated together with protons. The relativistic CR electron production by the shock is likely more inefficient than protons, and PIC simulations suggest that the number density at a given energy can be as low as $K_{ep} = N_{E_e}/N_{E_p} \sim$ 0.001 - 0.01 (Park et al. 2015), where N_{E_e} is the number spectrum of the relativistic electrons and E_e is the electron energy. Then, the CR electron luminosity at the GeV energy is estimated to be

$$L_e \approx \frac{\epsilon_e}{\epsilon_p} L_p \simeq 1.7 \times 10^{25}$$
(25)
 $\times \epsilon_{e,-4.5} l_{\text{loop},9.5}^2 B_{\text{rec},2}^3 n_{\text{rec},9}^{-1/2} \eta_{\text{rec},-1.5} f_{\text{nl},0.5} \text{ erg s}^{-1},$

where ϵ_e is the efficiency of CR electron production. We use $\epsilon_e = 10^{-1.5} \epsilon_p$ as a fiducial value (e.g., Maeda 2012), but the value of ϵ_e in non-relativistic shocks is highly uncertain. These relativistic electrons emit broadband photons via bremsstrahlung, synchrotron, and inverse Compton emissions.

4.1. Solar flares

The existence of non-thermal electrons is confirmed in solar flares (e.g., Holman et al. 2011; Oka et al. 2018), although the observed signals in hard X-ray bands are produced by non-relativistic electrons. The relativistic electrons are confined in the flare loop with a timescale of $t_{\rm esc}$ (see Equation (19)). We find that $t_{\rm esc}$ is much shorter than all the cooling timescales by bremsstrahlung, synchrotron, and inverse Compton processes. Therefore, the maximum energy of electrons should be the same as that of protons: $E_{e,\max} = E_{p,\max}$. Although this value of $E_{e,\max}$ seems to be higher than expected, the current hard X-ray and soft gamma-ray observations cannot constrain the maximum energy of electrons, because the photon spectrum exhibits no cutoff features below the MeV range (e.g., Lin et al. 2003).

We find that the emissions from relativistic electrons in the flare loops are challenging to detect. The bremsstrahlung and inverse Compton processes mainly produce GeV gamma rays, but they are fainter than the hadronic gamma rays. The synchrotron radiation spectrum has a peak at the soft X-ray band, which is easily overshone by thermal free-free emission by the evaporation plasma.

Nonthermal electrons produced in the solar corona move to the chromosphere and lose their energies via bremsstrahlung and Coulomb interactions (Brown 1971; Emslie 1978). This picture is consistent with the hard X-ray observations at footpoints of the flare loop (e.g., Holman et al. 2011). We should note that we cannot detect the bremsstrahlung photons by the relativistic electrons because of the relativistic beaming effect. Almost all photons are beamed toward the Sun due to their inefficient isotropization.

4.2. Protostellar flares

For protostellar flares, $B_{\rm rec}$ and $l_{\rm loop}$ are higher than those for solar flares. This leads to longer $t_{\rm esc}$ and $t_{\rm sh}$ and shorter $t_{\rm syn}$. We find that the synchrotron cooling is efficient for protostellar flares and other emission components are negligible for electrons of $E_e \gtrsim 5$ MeV. The maximum energy of CR electrons is given by the balance between synchrotron cooling and acceleration. The synchrotron cooling time is given as $t_{\rm syn} = 6\pi m_e c/(\sigma_T B_{\rm rec}^2 \gamma_e)$, where γ_e is the electron Lorentz factor and σ_T is the Thomson crosssection. This leads to the maximum electron Lorentz factor and synchrotron cutoff energy of

$$\gamma_{e,\max} = \sqrt{\frac{9\pi e \beta_A^2}{10\sigma_T \xi B_{\rm rec}}} \simeq 7.4 \times 10^4 B_{\rm rec,3}^{1/2} n_{\rm rec,10}^{-1/2} \xi_{0.3}^{-1/2},$$
(26)
$$E_{\gamma,\max} = \frac{he B_{\rm rec} \gamma_{e,\max}^2}{2\pi m_e c} \simeq 63 B_{\rm rec,3}^2 n_{\rm rec,10}^{-1} \xi_{0.3}^{-1} \,\,{\rm keV},$$
(27)

where $\beta_A = V_A/c$ and h is the Planck constant. Thus, non-thermal electrons emit broadband emission below hard X-ray bands. Equating $t_{\rm syn}$ and $t_{\rm esc}$, we obtain the cooling electron energy of $\gamma_{e,c} \simeq 23 l_{\rm loop,11}^{-1} B_{\rm rec,3}^{-2} \eta_{\rm turb,1}^{-1}$. The electron number spectrum has a break at $\gamma_e = \gamma_{e,c}$: $N_{\gamma_e} \propto \gamma_e^{-s}$ for $\gamma_e < \gamma_{e,c}$ and $N_{\gamma_e} \propto \gamma_e^{-s-1}$ for $\gamma_e > \gamma_{e,c}$ (e.g., Sari et al. 1998; Kimura et al. 2020).

The synchrotron-self absorption (SSA) is also efficient at low energies. This process shapes a low-energy cutoff in the non-thermal synchrotron spectra. We also estimate the optical depth for SSA (e.g., Rybicki & Lightman 1979),

$$\tau_{\rm ssa} = l_{\rm loop} \alpha_{\rm ssa} \nu^{-(p_e+4)/2}$$
(28)
$$\alpha_{\rm ssa} = \frac{\sqrt{3}e^3}{8\pi m_e} \left(\frac{3e}{2\pi m_e^3 c^5}\right)^{p_e/2} \left(\frac{\pi B_{\rm rec}}{4}\right)^{(p_e+2)/2}$$
$$\times C_{\rm ssa} \Gamma \left(\frac{3p_e+2}{12}\right) \Gamma \left(\frac{3p_e+22}{12}\right),$$
(29)

where $C_{\rm ssa} = L_e t_{\rm esc} E_{\rm min}^{p_e-2}/(l_{\rm loop}^2 l_{\rm nl})$ is the normalization factor for non-thermal electron spectrum, $p_e \approx s_{\rm inj} + 1$ is the electron spectral index after the cooling break, $\Gamma(x)$ is the Gamma function. Setting $\tau_{\rm ssa} = 1$, we estimate the SSA cutoff frequency to be

$$\nu_{\rm ssa} = (\alpha_{\rm ssa} l_{\rm out})^{2/(p_e+4)}$$
(30)
$$\simeq 66B_{\rm rec,3}^{11/7} n_{\rm rec,10}^{2/7} l_{\rm loop,11}^{2/7} \eta_{\rm rec,-1.5}^{2/7} \eta_{\rm turb,1}^{2/7} \epsilon_{e,-4.5}^{2/7} \text{ GHz},$$

where we use $p_e = 3$ for the estimate. We find that $\nu_{\rm ssa} \sim 1$ GHz for X-class solar flares and $\nu_{\rm ssa} \sim 100$ GHz for typical protostellar flares, as tabulated in Table 1. For the range of our investigation, the SSA cutoff frequency is close to or higher than the cooling frequency, $\nu_c = E_{\gamma,c}/h$. Then, the synchrotron spectrum can be approximately written by

$$E_{\gamma}L_{E_{\gamma}} \approx L_{\rm syn} \begin{cases} \left(\frac{E_{\gamma}}{E_{\gamma,\rm min}}\right)^2 \left(\frac{E_{\gamma,\rm min}}{E_{\gamma,\rm ssa}}\right)^{5/2} (E_{\gamma} < E_{\gamma,\rm min}) & \text{the} \\ \left(\frac{E_{\gamma}}{E_{\gamma,\rm ssa}}\right)^{5/2} & (E_{\gamma,\rm min} < E_{\gamma} < E_{\gamma,\rm ssa})^{0} \text{es} \\ 1 & (E_{\gamma,\rm ssa} < E_{\gamma} < E_{\gamma,\rm max}) \text{mm} \end{cases}$$

$$L_{\rm syn} \approx f_{\rm bol} L_e \simeq 3.5 \times 10^{29} l_{\rm loop,11}^2 B_{\rm rec,3}^3 n_{\rm rec,10}^{-1/2} \quad (32)$$
$$\times \epsilon_{e,-4.5} \eta_{\rm rec,-1.5} f_{\rm nl} f_{\rm bol,1} \ {\rm erg \ s^{-1}}$$

where $E_{\gamma,\text{syn,min}} = heB/(2\pi m_e c)$, $E_{\gamma,\text{ssa}} = h\nu_{\text{ssa}}$, and $f_{\text{bol}} = \ln(E_{\gamma,\text{max}}/E_{\gamma,\text{ssa}})$ is the bolometric correction factor (e.g., Kimura 2022).

For a quantitative prediction, we numerically integrate Equation (14) with a steady state assumption to obtain the non-thermal electron spectrum, and calculate the synchrotron spectrum by the method in Kimura et al. (2020); Kimura & Toma (2020). We take account of the SSA process by $E_{\gamma}L_{E_{\gamma}}|_{\text{obs}} = f_{\text{atn}}E_{\gamma}L_{E_{\gamma}}|_{\text{thin}}$, where $E_{\gamma}L_{E_{\gamma}}|_{\text{thin}}$ is the synchrotron spectra without the SSA process and $f_{\text{ssa}} \approx (1 - \exp(-\tau_{\text{ssa}}))/\tau_{\text{ssa}}$ is the absorption factor. Here, we ignore the heating by the SSA process for simplicity, which may modify the electron distribution and synchrotron spectrum around the SSA frequency (Ghisellini et al. 1988; Ghisellini & Svensson 1991).

Figure 4 shows the resulting radio to UV spectra from protostellar flares. The SSA cutoff appears around 100 - 1000 GHz in our models. As seen in the figure, the synchrotron spectra can be observable above the foreground signals (disk and jet components) for all the models in 10–100 GHz bands, despite that the SSA is effective in the band. T-Tauri stars (class II/III YSOs) exhibit flares in mm and sub-mm bands (Bower et al. 2003; Massi et al. 2006; Mairs et al. 2019; Naess et al. 2021). These mm and sub-mm flares can be interpreted as the synchrotron emission by relativistic electrons accelerated during the stellar flares. The observed luminosities for mm/sub-mm flares are $\nu L_{\nu} \sim 10^{29} - 10^{31} \text{ erg s}^{-1}$, which is consistent with our model predictions. The spectral break by synchrotron emission in mm/submm bands can be useful to estimate the magnetic field strength and/or non-thermal electron number density, as shown in Figure 4. This method is used in solar flares (Fleishman et al. 2022). Future multi-band surveys together with detailed modeling of non-thermal emission will be able to unravel the non-thermal phenomena during the YSO flares. We should note that the triggering mechanism of T-Tauri flares is expected to be similar to that of solar flares, because T-Tauri flares have X-ray features similar to those of main sequence stars (Getman & Feigelson 2021). However, T-Tauri stars likely have strong magnetic fields and large flare loops, which are nparable to those for protostellar flares. Therefore, mm/sub-mm emission from T-Tauri flares should similar to those for our Model A and B.

^{ssa)} The timescales of radio flares observed in mm/subnax)mm bands vary greatly among the events (e.g., Naess et al. 2021). Some show minutes-scale variability, which is consistent with our model prediction. Recently, minutes-scale stellar flares are also observed in optical band (Aizawa et al. 2022), although these are from M dwarfs. Others show variability on a timescale of a few days, which is probably caused by time-variable accretion.

The synchrotron fluxes in the infrared to optical bands are much lower than that by the protostar. The synchrotron spectrum is stronger than the protostar component in UV and very soft X-ray ranges, but these signals are completely attenuated due to dense envelopes. The synchrotron spectrum extends to hard X-ray and MeV ranges as seen in Figure 4. However, the hard Xray flux is lower than the thermal X-ray emission (see Section 3), and the MeV flux is lower than the sensitivity of future satellites, such as e-ASTROGAM (De Angelis et al. 2017), AMEGO (McEnery et al. 2019), and GRAMS (Aramaki et al. 2020).

5. DISCUSSION

5.1. Cosmic-rays in molecular clouds

Aharonian et al. (2020); Baghmanyan et al. (2020) found that the CR density above $\sim 10 \text{ GeV}$ in some molecular clouds is higher than that in the local interstellar medium (ISM) by a factor of a few. This may indicate the existence of sources of CRs of $E_p \gtrsim 100 \text{ GeV}$ in molecular clouds. On the other hand, HAWC Collaboration also put constraints on multi-TeV gamma-ray flux from giant molecular clouds (Albert et al. 2021), implying that there are no strong sources of CRs of $E_p \gtrsim 10$ TeV. Our model predicts that protostellar flares can accelerate CRs above 10 TeV with a total CR energy of $\mathcal{E}_p \sim 10^{35} - 10^{38}$ erg, depending on the model parameters of protostellar flares. If some fraction of CRs escape from the flare loop, they diffuse into the molecular clouds and emit GeV-TeV gamma rays there via hadronuclear interactions. Also, these CRs may be ionization and heating sources of molecular clouds (Umebayashi & Nakano 1981; Padovani et al. 2009; Fitz Axen et al. 2021). Indeed, estimates of the CR ionization rate by interstellar chemistry modeling indicate that CR energy densities in dense clouds should be higher than that in local ISM (Padovani et al. 2020). Below, we roughly estimate the CR energy density in a molecular cloud provided by protostellar flares.

We consider that a typical molecular cloud of size $R_{\rm cl} \sim 10 \ {\rm pc}$ contains $N_{\rm ps} \sim 100 \ {\rm protostars}$, as in L1688 in Rho Ophiuchi (Wilking et al. 2008). The flare interval timescale on a single protostar will depend on the details of the interaction between the protostar and the innermost disk. The Chandra Orion Ultradeep Project (COUP), which was a two-week X-ray monitoring campaign by Chandra toward the Orion Nebula Cluster, found that a high detection rate ($\gtrsim 50\%$) of X-rays in class-I protostars (Prisinzano et al. 2008). This suggests that protostars produce at least one huge flare per two weeks. We estimate the differential CR generation rate in the molecular cloud to be $E_p L_{E_p} \approx$ $\mathcal{E}_p N_{\rm ps} f_{\rm bol} f_{\rm esc} / t_{\rm intvl} \sim 10^{30} - 10^{33} f_{\rm esc} f_{\rm bol,-1} \, {\rm erg \ s^{-p}}^{-1}$ where $f_{\rm esc}$ is the escape fraction from the flare loop, $f_{\rm bol} \approx 1/\ln(E_{p,\rm max}/{\rm GeV})$ is the bolometric correction factor, and we approximate $s \approx 2$. Balancing the CR injection to and escape from the molecular cloud, the differential CR energy density is estimated to be (e.g., Kimura et al. 2018b)

$$E_p U_{E_p} \sim \frac{E_p L_{E_p}}{R_{\rm cl} D_p} \tag{33}$$

$$\sim 7 \times 10^{-8} - 7 \times 10^{-5} \left(\frac{E_p}{\text{TeV}}\right)^{-1/3} \text{eV cm}^{-3}$$

where we use a canonical diffusion coefficient of $D_p \sim 3 \times 10^{29} (E_p/\text{TeV})^{1/3} \text{ cm}^2 \text{ s}^{-1}$ (e.g., Strong et al. 2007). These values are much lower than the CR energy density in ISM, $U_{\text{CR,ISM}} \sim 3 \times 10^{-3}$ eV cm⁻³ at 1 TeV (e.g., Aguilar et al. 2015). Thus, protostellar flares are unlikely to be the source of the CR excess in molecular clouds, unless the diffusion coefficient in molecular clouds is orders of magnitude lower than the canonical value.

5.2. Cosmic rays in protoplanetary disks

Cosmic rays accelerated at the flare can be the ionization source in protoplanetary disks. Previous studies assumed that protostellar flares produce CRs of MeV-GeV energies (e.g., Feigelson et al. 2002b; Padovani et al. 2018). These CRs can be an important ionization source of the disk surface (Turner & Drake 2009; Rab et al. 2017; Fraschetti et al. 2018), or even at the midplane if we assume efficient diffusion (Rodgers-Lee et al. 2020). Our model suggests that protostellar flares produce CRs of much higher energies ($\sim 0.1 - 1$ TeV). These CRs have a higher penetration power and diffuse faster than the lower-energy CRs. These features are advantageous for ionizing the disk midplane. However, Fujii & Kimura (2022) recently showed that intrusion of CRs to the disk midplane is more challenging than previously thought because CRs usually propagate along the sheared magnetic field configuration (see also Silsbee et al. 2018, for discussions on the propagation of CRs into a disk). The ionization rate by the CRs from protostellar flares should be investigated carefully by considering the propagation of high-energy CRs in a realistic magnetic field geometry.

CRs from protostars can produce short-lived radioactive nuclei, e.g., Al^{26} and Be^{10} , which can be an important ionization source at the inner part of protoplanetary disks. Previous studies considered CR production at accretion shocks (Gaches et al. 2020) or utilized the empirical relation obtained from solar flare observations (Jacquet 2019). Our model proposes that accretiondriven protostellar flares can also be an efficient CR accelerator, and the effects of these CRs should be examined near future.

5.3. Attenuation of TeV gamma rays

VHE gamma rays can be attenuated by the twophoton interactions $(\gamma \gamma \rightarrow e^+ e^-)$ if copious low-energy photons exist. We estimate the optical depth for twophoton interactions, $\tau_{\gamma\gamma}$. The flare loop is surrounded by the protostar and optically thick accretion disk, both

of which emit thermal photons. Assuming that the temperatures of the protostar and the disk are $T_* =$ 4000 K, the typical energy of the thermal photons is $E_{\gamma,*} \approx 2.8 k_B T_* \sim 1(T_*/4000 \text{ K}) \text{ eV}$. Then, gamma rays of $E_{\gamma} \sim 1 (T_*/4000 \text{ K})^{-1}$ TeV efficiently interact with the thermal photons. The number density of the thermal photons is estimated to be $n_{\gamma,*} \approx a_{\rm rad} T_*^4 / E_{\gamma,*} \simeq$ $1.3 \times 10^{12} (T_*/4000 \text{ K})^3 \text{ cm}^{-3}$. This results in $\tau_{\gamma\gamma} \approx$ $0.2\sigma_T n_{\gamma,*} l_{\text{loop}} \simeq 0.017 (T_*/4000 \text{ K})^3 l_{\text{loop},11}$. Therefore, TeV gamma rays likely escape from the system without attenuation by two-photon interactions. The inner part of protoplanetary disks may be hotter than the protostellar surface, and it can reach $\sim 2 \times 10^4$ K (Popham et al. 1993). In this case, $\tau_{\gamma\gamma} > 1$ is satisfied above ~ 0.2 TeV, and detection of very-high-energy gamma rays from protostellar flares is challenging (see also del Valle et al. 2011 for discussion on $\tau_{\gamma\gamma}$ with a different photon field).

5.4. Implications for the driving mechanism of protostellar flares

Hosokawa & Omukai (2009) suggested that in the early evolutionary stage, a protostar does not have a surface convective layer depending on the accretion history. As the surface convective layer would be crucial for the magnetic activity mediated by the stellar dynamo, we cannot expect dynamo-origin flares in the absence of the convective layer. Thus, class-0 objects are unlikely to produce powerful flares by magnetospheric models. On the other hand, class-0 objects should exhibit strong flaring activities in our accretion-driven flare model. Since class-0 objects are highly obscured in soft X-rays (Grosso et al. 2020), we need to rely on non-thermal signatures in mm/sub-mm and gamma-ray bands to probe the flaring activities in class-0 objects. A monitoring campaign of nearby class-0 objects would test the stellar evolution scenario and unravel the mechanism of flaring activities of protostars.

Our scenario of protostellar flares creates a cavity in the inner part of the protoplanetary disk. This may induce time variability in the near-infrared band, with a typical timescale of a few days (Takasao et al. 2019). Such a time variability is observed in infrared by Hershel (Billot et al. 2012). The dust in protoplanetary disks can be observed in GHz-radio bands, and the angular resolution of ngVLA can be 0.01 - 0.1 AU scale for a distance of ~ 150 pc. Hence, ngVLA may directly resolve the cavity. In our scenario, the size of the cavity may be larger than the magnetospheric models, and thus, future radio observations coordinated with X-ray satellites will reveal the protostellar flare mechanism.

6. SUMMARY

We developed models for the gamma-ray emissions from solar and protostellar flares. The model for solar flares are based on a standard solar flare model, and the model for protostellar flares assumes the flare mechanism proposed by Takasao et al. (2019). In both models, we expect the formation of X-ray luminous flare loops on the stellar surface as a result of magnetic reconnection. We hypothesize that CR protons are produced at the termination shock and are injected to the flare loops. We examine the high-energy gamma-ray production via hadronuclear interactions with the evaporation plasma. Our model can reproduce the gamma-ray data of solar flares and roughly be consistent with the X-ray data of the same flare. We applied this model to protostellar flares. As a result, we found that CTA can detect VHE gamma rays from a single protostellar flare if the CR production is more efficient in protostellar flares than solar flares (Model C). If the CR production efficiency is the same as that for solar flares (Models A and B), VHE gamma-ray detection is challenging near future. Emission by non-thermal electrons accelerated together with protons are also detectable in mm/sub-mm bands for all the models. The duration of the mm/sub-mm flare is $t_{\gamma} \sim 10^3$ sec, while the time interval between the flare could be $t_{intvl} \gtrsim 10^6$ sec (see Section 5 for the time interval). The duty cycle of the mm/sub-mm flare is $t_{\gamma}/t_{\rm intvl} \lesssim 10^{-3}$. Thus, dedicated strategic observations are necessary to identify the mm/sub-mm flares from protostars.

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